

## Real-Time Collision Detection for Dynamic Virtual Environments

### Distance Fields



Arnulph Fuhrmann

Fraunhofer Institute for Computer  
Graphics  
Darmstadt, Germany

IEEE Virtual Reality 2005 – March 13, 2005 - Bonn, Germany

### Outline

- Introduction
- Distance Field Generation
- Collision Detection using Distance Fields
- Conclusion

Arnulph Fuhrmann - afuhr@igd.fhg.de

### Introduction

- Physically based modeling
  - Cloth, hair, etc.
- Problem
  - Many contact points
- During Simulation
  - Detect Collision
  - Compute Collision Response
    - Proximity or penetration depth
    - Surface normal



Arnulph Fuhrmann - afuhr@igd.fhg.de

### Distance Field Definition

- Scalar function

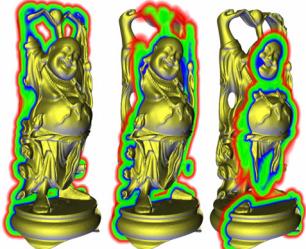
$$D : \mathbb{R}^3 \rightarrow \mathbb{R}$$

- $dist(\mathbf{p})$  = distance to closest point on surface
- $sign(\mathbf{p})$  = negative if inside object

$$D(\mathbf{p}) = sign(\mathbf{p}) \cdot dist(\mathbf{p})$$

Arnulph Fuhrmann - afuhr@igd.fhg.de

## Example – Distance Field 2D-Slices



Arnulph Fuhrmann - afuhr@igd.fhg.de



## Outline

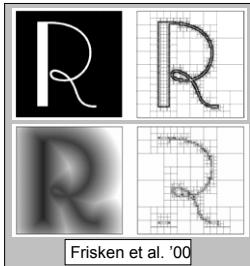
- Introduction
- **Distance Field Generation**
- Collision Detection using Distance Fields
- Conclusion

Arnulph Fuhrmann - afuhr@igd.fhg.de



## Distance Field Data Structures

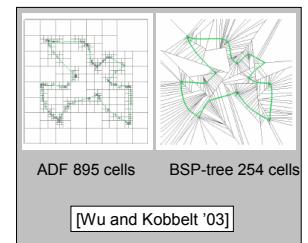
- Uniform 3D grid
  - Queries take  $O(1)$  time
  - Curved surfaces can be represented quite well
  - $C^0$  continuous
- Adaptively sampled distance fields (ADFs)
  - [Friskin et al. '00]
  - $C^{-1}$  between different levels
    - can be resolved



Arnulph Fuhrmann - afuhr@igd.fhg.de

## Distance Field Data Structures

- BSP-tree
  - [Wu and Kobbelt '03]
  - Piecewise linear approximation
  - Generation computationally expensive
  - Discontinuities between cells
  - Compact!



Arnulph Fuhrmann - afuhr@igd.fhg.de



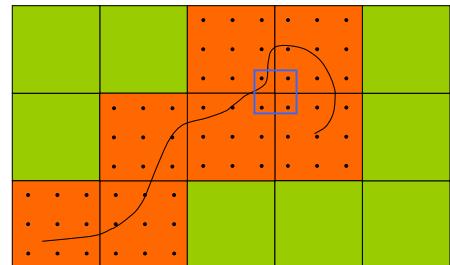
## Distance Field Data Structures

- Sparse Block Grids
  - [Bridson '03]
  - Distance values needed only for a small band
- Divide the uniform grid into blocks
  - Coarse grid contains pointers to fine sub-grids
  - Not all sub-grids exist
- Queries (in comparison to uniform grids)
  - More complex
  - Less efficient

Arnulph Fuhrmann - afuhr@igd.fhg.de



## Sparse Block Grid Example



Arnulph Fuhrmann - afuhr@igd.fhg.de



## Sparse Block Grid – Memory Savings

- Uniform Grid
  - Resolution 378x396x81
  - 48.5 MB
- Sparse Block Grid
  - Same resolution
  - 3x3x3 sub-grids
  - 6.7 MB
  - 86% memory savings



Arnulph Fuhrmann - afuhr@igd.fhg.de

## Computation of Distance Fields

- Object representation
  - Triangular mesh
- Problem
  - Computing distances for all grid points
  - Naïve computation too costly
- Collision detection
  - Only a small band needed



Arnulph Fuhrmann - afuhr@igd.fhg.de



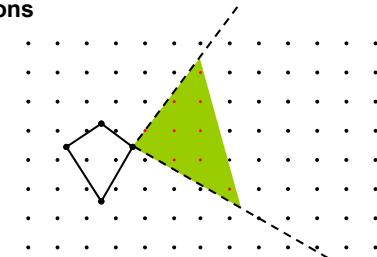
## Computation of Distance Fields

- Propagation methods
  - Fast Marching methods [Sethian '96]
  - Distance Transforms [Jones and Satherley '01]
- Rasterizing of distance functions
  - Full distance field
  - [Sud et al. '04], [Hoff et al. '99]
- Bounded Voronoi Regions
  - [Sigg et al. '03], [Breen et al. '01]
  - Bounding polyhedron around Voronoi regions of edges, faces and vertices

Arnulph Fuhrmann - afuhr@igd.fhg.de



## Scan Conversion of Bounded Voronoi Regions



Arnulph Fuhrmann - afuhr@igd.fhg.de



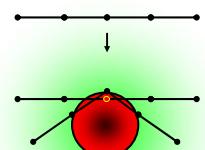
## Outline

- Introduction
- Distance Field Generation
- Collision Detection using Distance Fields
- Conclusion

Arnulph Fuhrmann - afuhr@igd.fhg.de

## Collision Detection

- [Fuhrmann et al. '03]
- Scenario
  - Deformable object A
  - Static object B
- Collision Detection
  - Sample object A
  - Test sample points for collision with B
- If both objects are deformable
  - Swap and repeat



Arnulph Fuhrmann - afuhr@igd.fhg.de



## Collision Detection

- Problem
  - Edges intersect object
- Solution
  - Preserve & distance at vertices



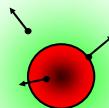
Arnulph Fuhrmann - afuhr@igd.fhg.de



## Queries needed for collision detection

(On a uniform or sparse grid)

- Distance
  - Tri-linear interpolation
- Normal
  - Direction given by the gradient

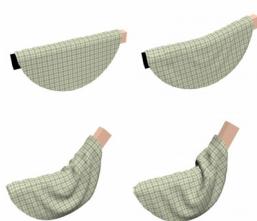


Arnulph Fuhrmann - afuhr@igd.fhg.de



## What about deforming collision objects?

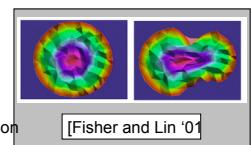
- Multiple distance fields
- Linked rigid objects
  - One distance field per object
- Not possible yet
  - Soft objects like a bending human arm



Arnulph Fuhrmann - afuhr@igd.fhg.de

## Other approaches for deforming objects

- [Bridson et al. '03]
  - Clothing and animated characters
  - Pre-computed ADFs for the body parts
  - Can be used for several cloth simulations
- [Fisher and Lin '01]
  - Deforming geometries
  - Collision detection is done hierarchically
  - Partial DF updates only
  - Internal distance fields for collision response

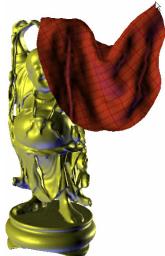


Arnulph Fuhrmann - afuhr@igd.fhg.de



## Demo Video

- Captured directly from screen
- Simulation runs in java 1.4.1
- Rendering with OpenGL
- Tests made on a Intel Processor at 2.8 GHz
- Buddha model consist of 100k triangles



Arnulph Fuhrmann - afuhr@igd.fhg.de



## Real-Time Collision Detection using Distance Fields

Arnulph Fuhrmann  
Martin Knuth

## Outline

- Introduction
- Distance Field Generation
- Collision Detection using Distance Fields
- Conclusion



Arnulph Fuhrmann - afuhr@igd.fhg.de

## Summary

- Distance Fields Generation
  - Pre-Processing step
  - Duration: Some seconds
- Collision Detection using Distance Fields
  - Most useful for deformable against rigid objects
  - Efficient computation of
    - Penetration depth / proximity
    - Gradient (Normal)
  - Easy to implement
  - Robust algorithm



Arnulph Fuhrmann - afuhr@igd.fhg.de

## Thank You!

Arnulph Fuhrmann - afuhr@igd.fhg.de

- [Friskin et al. '00] Sarah F. Friskin, Ronald N. Perry, Alyn P. Rockwood, and Thouis R. Jones. Adaptively Sampled Distance Field. SIGGRAPH 2000, pages 249–254.
- [Wu and Kobbelt '03] Jianhua Wu, and Leif Kobbelt. Piecewise Linear Approximation of Signed Distance Fields. In Vision, Modeling and Visualization 2003 Proceedings, pages 513–520.
- [Bridson '03] Robert Bridson. Computational aspects of dynamic surfaces. PhD Thesis, Stanford University, 2003.
- [Sethian '96] J.A. Sethian. A Fast Marching Level Set Method for Monotonically Advancing Fronts. Proceedings of the National Academy of Science, 93(4):1591–1595, 1996.
- [Jones and Satherley '01] Mark W. Jones, and Richard Satherley. Using Distance Fields for Object Representation and Rendering. In Proc. 19th Ann. Conf. of Eurographics (UK Chapter), pages 37–44, 2001.
- [Sud et al. '04] Avneesh Sud, Miguel A. Otaduy and Dinesh Manocha. DiFi: Fast 3D Distance Field Computation Using Graphics Hardware. Eurographics 2004.
- [Hoff et al. '99] K. E. Hoff III, J. Keyser, M. Lin, D. Manocha, and T. Culver. Fast computation of generalized Voronoi diagrams using graphics hardware. In Proceedings of ACM SIGGRAPH 1999, pages 227–230.
- [Sigg et al. '03] Christian Sigg, Ronald Peikert, and Markus Gross. Signed Distance Transform Using Graphics Hardware. In Proceedings of IEEE Visualization '03.
- [Breen et al. '01] David E. Breen, Sean Mauch, Ross T. Whitaker, and Jia Mao. 3D Metamorphosis Between Different Types of Geometric Models. Eurographics 2001 Proceedings, 20(3):36–48.
- [Fuhrmann et al. '03] Arnulph Fuhrmann, Gerrit Sobotta, and Clemens Gross. Distance Fields for Rapid Collision Detection in Physically Based Modeling. In Proceedings of GraphCon 2003, pages 58–65.
- [Bridson et al. '03] Robert Bridson, S. Marino, and Ronald Fedkiw. Simulation of clothing with folds and wrinkles. In Proc. ACM/Eurographics Symposium on Computer Animation, pages 28–36, 2003.
- [Fisher and Lin '01] S. Fisher, and M. Lin. Deformed distance fields for simulation of non-penetrating flexible bodies. In Proc. of Eurographics Workshop on Geometric Modelling and Simulation, 2001.