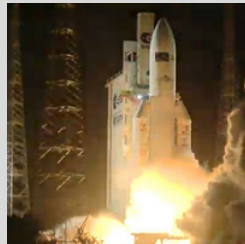


Systems of High Safety and Security

Lecture 3 from 29.10.2025: The Development Process

Winter term 2025/26



Christoph Lüth

Organisatorisches

- ▶ Die Vorlesung und Übung am 05.11.2025 **fällt aus.**

Software Development Models

Software Development Process

- ▶ A software development process is the **structure** imposed on the development of a software product.
- ▶ We classify processes according to **models** which specify
 - ▶ the artefacts of the development: the software product itself, specifications, test documents, reports, reviews, proofs, plans etc;
 - ▶ the different stages of the development;
 - ▶ and the artefacts associated to each stage.
- ▶ Different models have a different focus: correctness, development time, flexibility.
 - ▶ Note you cannot have all three
- ▶ What does **quality** mean in this context?
 - ▶ What is the **output** — just the software product, or more? (specifications, test runs, documents, proofs. . .)

Artefacts in the Development Process

Planning:

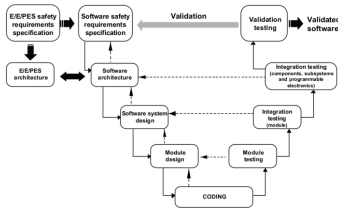
- ▶ Document plan
- ▶ V&V plan
- ▶ QM plan
- ▶ Test plan
- ▶ Project manual

Specifications:

- ▶ Requirements
- ▶ System specification
- ▶ Module specification
- ▶ User documents

Implementation:

- ▶ Source code
- ▶ Models
- ▶ Documentation



Verification & validation:

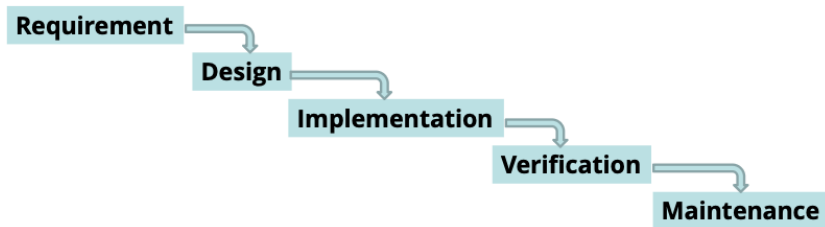
- ▶ Code review protocols
- ▶ Test cases, test results
- ▶ Proofs

Possible formats:

- ▶ Documents:
 - ▶ Word/LaTeX documents
 - ▶ Excel sheets
 - ▶ Wiki text
 - ▶ Database (Doors)
- ▶ Models:
 - ▶ UML/SysML diagrams
 - ▶ Formal languages: Z, HOL, B, etc.
 - ▶ Matlab/Simulink or similar diagrams
- ▶ Source code

Waterfall Model (Royce 1970)

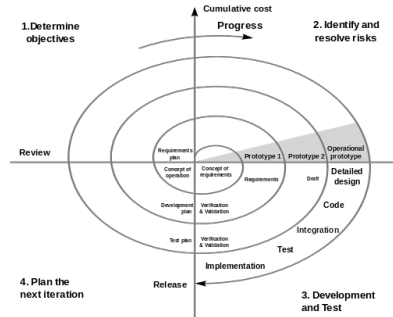
- ▶ Classical top-down sequential workflow with strictly separated phases.



- ▶ Unpractical as an actual workflow (no feedback between phases), but even the original paper did **not** really suggest this.

Spiral Model (Böhm 1986)

- ▶ Incremental development guided by **risk factors**
- ▶ Four phases:
 - ▶ Determine objectives
 - ▶ Analyse risks
 - ▶ Development and test
 - ▶ Review, plan next iteration
- ▶ See e.g.
 - ▶ Rational Unified Process (RUP)
- ▶ Drawbacks:
 - ▶ Risk identification is the key, and can be quite difficult



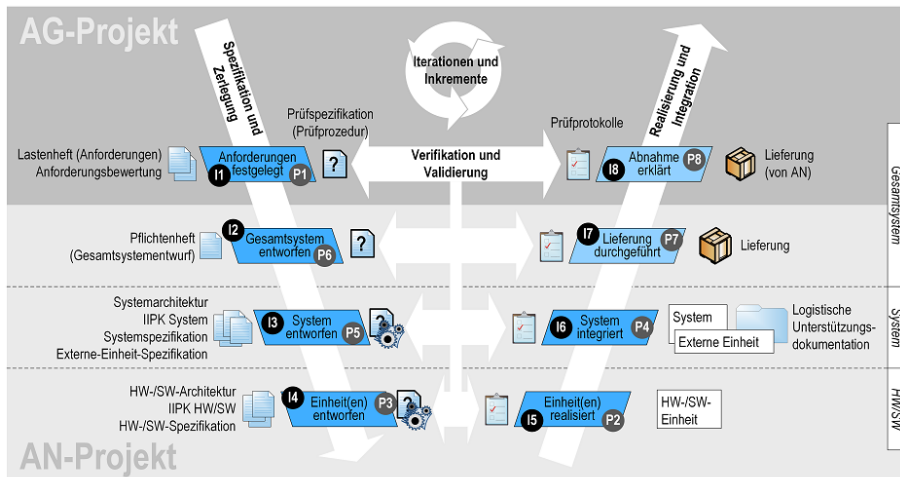
Agile Methods

- ▶ **Prototype-driven** development
 - ▶ e.g. Rapid Application Development
 - ▶ Development as a sequence of prototypes
 - ▶ Ever-changing safety and security requirements
- ▶ **Agile programming**
 - ▶ e.g. extreme Programming (XP), Scrum
 - ▶ Development guided by functional requirements
 - ▶ Process structured by rules of conduct for developers
 - ▶ Rules capture best practice
 - ▶ Less support for non-functional requirements
- ▶ **Test-driven development (TDD)**
 - ▶ Tests as **executable specifications**: write tests first
 - ▶ Often used together with the other two

V-Model

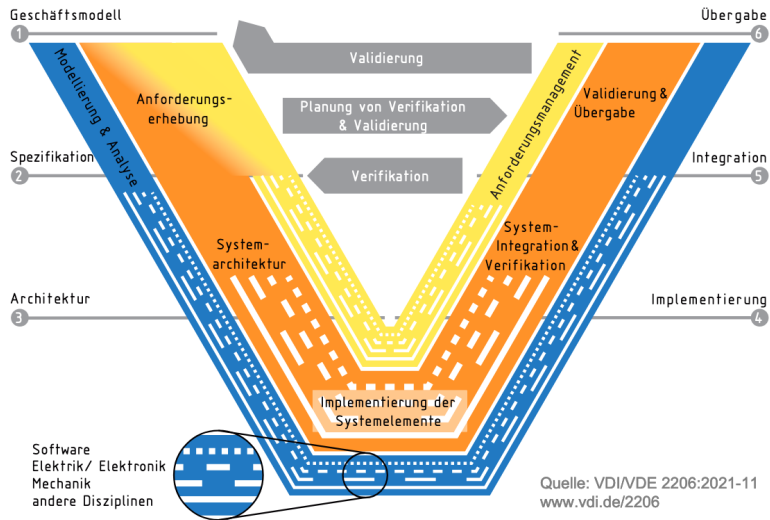
- ▶ Evolution of the waterfall model:
 - ▶ Each phase supported by corresponding verification & validation phase
 - ▶ Feedback between next and previous phase
- ▶ Standard model for public projects in Germany
 - ▶ ... but also a general term for models of this shape.
- ▶ Current: V-Modell XT (“extreme tailoring”)
 - ▶ Shape gives **dependencies**,
 - ▶ **not** necessarily **development timeline**.

Variations of the V-Modell: CIO Bund

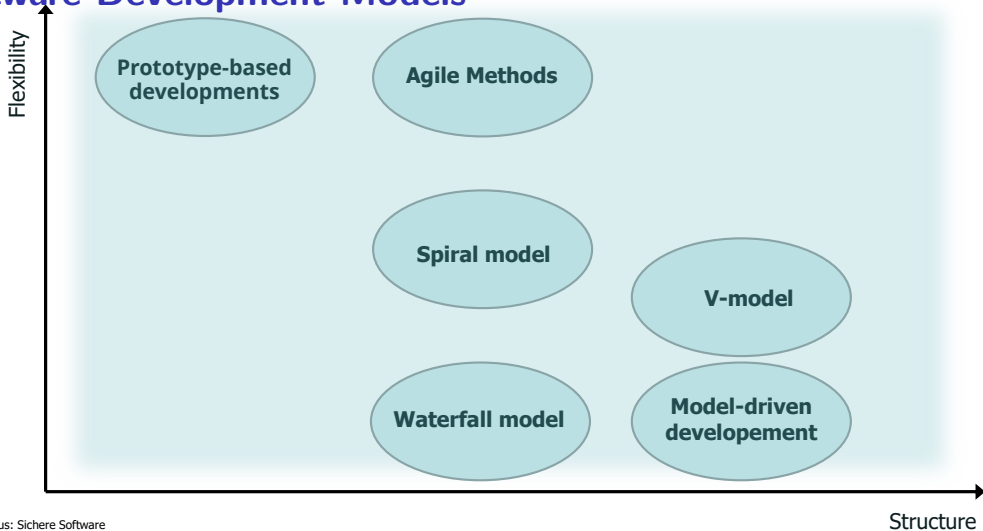


Quelle: <https://www.cio.bund.de/>, Beauftragter der Bundesregierung für IT

Variations of the V-Modell: VDI/VDE



Software Development Models



Development Models for Safety-Critical Systems

Development Models for Critical Systems

- ▶ Ensuring safety/security needs structure.
 - ▶ ... but **too much** structure makes developments bureaucratic, which is **in itself** a safety risk.
 - ▶ Cautionary tale: Ariane-5
- ▶ Standards put emphasis on **process**.
 - ▶ Everything needs to be planned and documented.
 - ▶ Key issues: **auditability**, **accountability**, **traceability**.
- ▶ Best suited development models are **variations of the V-model** or spiral model.
- ▶ A new trend? V-Model XT allows variations of original V-model, e.g.
 - ▶ V-Model for initial developments of a new product,
 - ▶ Agile models (e.g. Scrum) for maintenance and product extensions.

Auditability and Accountability

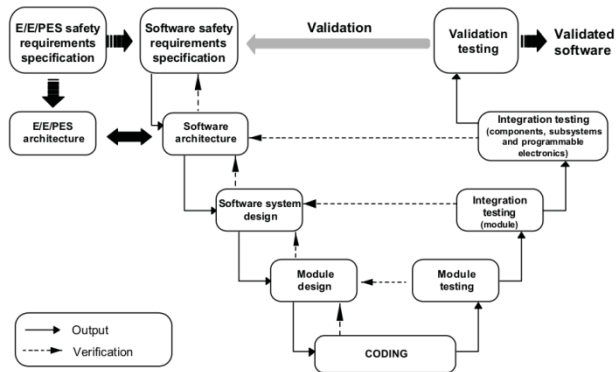
- ▶ **Version control and configuration management** is **mandatory** in safety-critical development (auditability).
- ▶ Keeping track of all artifacts contributing to a particular instance (**build**) of the system (**configuration, baseline**), and their **versions**.
- ▶ **Repository** keeps **all artifacts** in **all versions**.
 - ▶ Centralised (one repository) vs. distributed (every developer keeps own repository)
 - ▶ General model: check out – modify – commit – draw baseline
 - ▶ Baseline: identification of artefacts that are part of the same product release
 - ▶ Concurrency: enforced **lock**, or **merge** after commit.
- ▶ Well-known systems:
 - ▶ Commercial (all outdated): ClearCase, Perforce, Bitkeeper. . .
 - ▶ Open Source: **git** (outdated: svn, cvs, Mercurial)

Traceability

- ▶ The idea of being able to **follow requirements** (in particular, safety requirements) from requirement spec **to the code** (and possibly back).
- ▶ On the simplest level, an Excel sheet with (manual) links to the program.
- ▶ More sophisticated tools (e.g. DOORS):
 - ▶ Decompose requirements, hierarchical requirements
 - ▶ Two-way traceability: from code, test cases, test procedures, and test results back to requirements
 - ▶ e.g. RTCA DO-178C requires that all code is derived from requirements
- ▶ The SysML modelling language has traceability support:
 - ▶ Each model element can be traced to a requirement.
 - ▶ Special associations to express traceability relations.

Development Model in IEC 61508

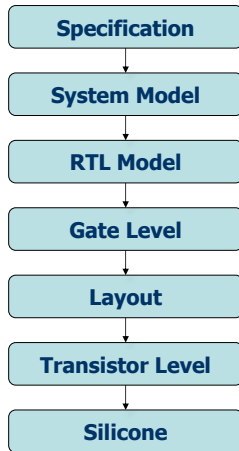
- ▶ IEC 61508 is agnostic with respect to the development model, but:
 - ▶ safety-directed activities are required for each phase of the life cycle (**safety life cycle**).
 - ▶ Development is one part of the life cycle.
- ▶ The only development model mentioned is a V-model:



Development Model in DO-178C

- ▶ DO-178C defines different **processes** in the SW life cycle:
 - ▶ Planning process
 - ▶ Development process, structured in turn into
 - ▶ Requirements process
 - ▶ Design process
 - ▶ Coding process
 - ▶ Integration process
 - ▶ Verification process
 - ▶ Quality assurance process
 - ▶ Configuration management process
 - ▶ Certification liaison process
- ▶ There is no conspicuous diagram, but the Development Process has sub-processes suggesting the phases found in the V-model as well.
 - ▶ Implicit recommendation of the V-model.

Development Model for Hardware



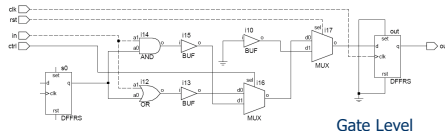
```
SC_MODULE(example) {  
  sc_in_clk clk;  
  sc_in<bool> rst, in, ctrl; sc_out<bool> out;  
  int o, s0;
```

```
  void tick() {  
    if (rst.read()) o = 0;  
    else if (!ctrl.read()) o = s0 | in.read();  
    else o = s0 & in.read();  
    out.write(o); s0 = o;  
  }  
  ...  
}
```

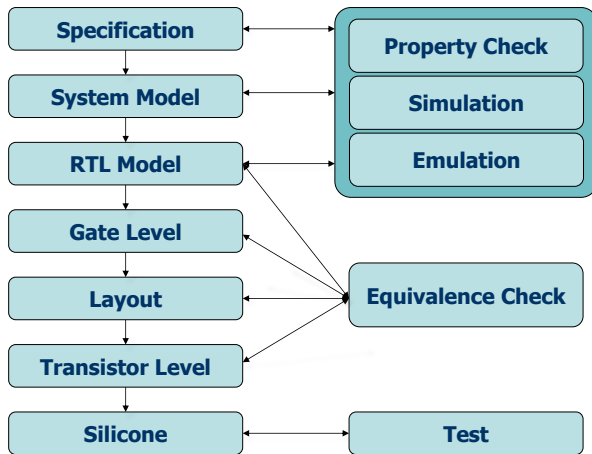
System-Model: SystemC

```
always @(posedge clk)  
  if (rst) out <= 0;  
  else  
    if (!ctrl) out <= s0 | in;  
    else out <= s0 & in;
```

Register-Transfer-Ebene: Verilog



Development Model for Hardware

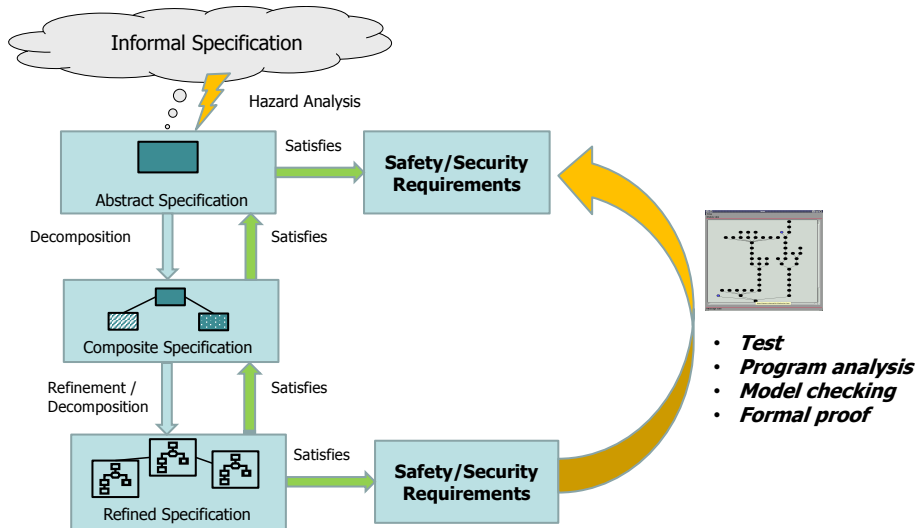


Basic Notions of Formal Software Development

Formal Software Development

- ▶ In a formal development, properties are stated in a rigorous way with a **precise mathematical semantics**.
- ▶ Formal specification requirements can be **proven**.
- ▶ **Advantages** :
 - ▶ Errors can be found early in the development process.
 - ▶ High degree of confidence into the system.
 - ▶ Recommended for high SILs/EALs.
- ▶ **Drawbacks** :
 - ▶ Requires a lot of effort and is thus expensive.
 - ▶ Requires qualified personnel (that would be **you**).
- ▶ There are tools which can help us by
 - ▶ finding (simple) proofs for us (model checkers), or
 - ▶ checking our (more complicated) proofs (theorem provers).

Structuring the Formal Development



Finite State Machines

Finite State Machine (FSM)

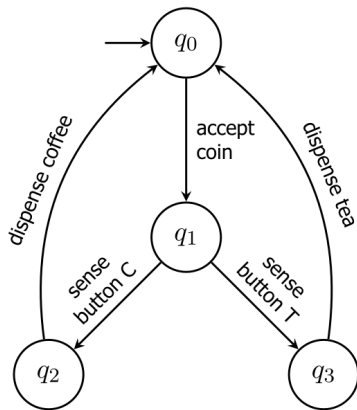
A FSM is given by $\mathcal{M} = \langle \Sigma, \Sigma_0, \rightarrow \rangle$ where

- ▶ Σ is a finite set of **states**,
- ▶ $\Sigma_0 \subseteq \Sigma$ is a set of **initial states**, and
- ▶ $\rightarrow \subseteq \Sigma \times \Sigma$ is a **transition relation**, such that \rightarrow is left-total:

$$\forall s \in \Sigma. \exists s' \in \Sigma. s \rightarrow s'$$

- ▶ The most basic notion of a system.
- ▶ Many variations of this definition exists, e.g. no initial states, state variables or labelled transitions.
- ▶ Note there is no input or output, and no **final** state (key difference to automata).
- ▶ If \rightarrow is a function, the FSM is **deterministic**, otherwise it is **non-deterministic**.

Example: Vending Machine



Transitions:

- 1 Insert/accept coin
- 2 Press/sense button: tea or coffee
- 3 Dispense tea or coffee, return to (1)

$$\mathcal{M} = \langle Q, Q_0, \rightarrow \rangle$$

$$Q = \{q_0, q_1, q_2, q_3\}$$

$$Q_0 = \{q_0\}$$

$$\rightarrow = \{(q_0, q_1), (q_1, q_2), (q_1, q_3), (q_2, q_0), (q_3, q_0)\}$$

Traces

Trace

Given a set Σ of states, a (finite) **trace** is a (finite) sequence $t = \langle t_0, t_1, t_2, \dots, t_n \rangle$ with $t_i \in \Sigma$.

A trace is **admissible** for a FSM $\mathcal{M} = \langle \Sigma, \Sigma_0, \rightarrow \rangle$ iff

- i $t_0 \in \Sigma_0$, and
- ii $\forall i. i < n \implies t_i \rightarrow t_{i+1}$.

- ▶ The empty sequence $\varepsilon = \langle \rangle$ is the empty trace. It is admissible for all FSMs.
- ▶ For a (finite) trace $t = \langle t_i \rangle_{i=0, \dots, n}$, we write $t[i]$ for t_i .
- ▶ The set of all **finite** traces for Σ is written Σ^* ; the set of **infinite** traces is written Σ^ω , and the set of **all** traces is written $\text{Tr}(\Sigma) = \Sigma^* \cup \Sigma^\omega$.

Trace Algebra

- For a (finite) trace $t = \langle t_i \rangle_{i=0, \dots, n}$, we define the **length** of t as $|t| \stackrel{\text{def}}{=} n + 1$, with $|\varepsilon| = 0$.

Concatenation

Given a (finite) trace s , and a (finite) trace t , their **concatenation** $s \cdot t$ is defined as

$$(s \cdot t)[j] \stackrel{\text{def}}{=} \begin{cases} s[j] & j < |s| \\ t[j - |s|] & j \geq |s| \end{cases}$$

- Concatenation can be generalised to **sets** of traces, with $S \cdot T \stackrel{\text{def}}{=} \{s \cdot t \mid s \in S, t \in T\}$.

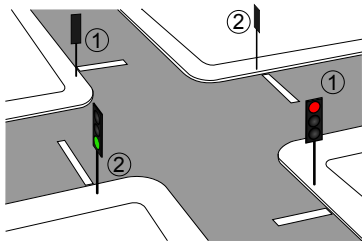
Prefix Ordering

A trace t is a **prefix** of a trace s , written $t \leq s$, iff $\exists t'. t \cdot t' = s$.

- The prefix ordering generalises to **sets** of traces by $T \leq S$ iff $\forall t. t \in T \implies \exists s. s \in S \wedge t \leq s$.

Example: Street Crossing with Traffic Lights

► States and Transitions:



Source: Wikipedia

$$\mathcal{M} = \langle Q, Q_0, \rightarrow \rangle$$

$$L = \{r, ry, y, g\}$$

$$Q = L \times L$$

$$Q_0 = \{\langle r, g \rangle\}$$

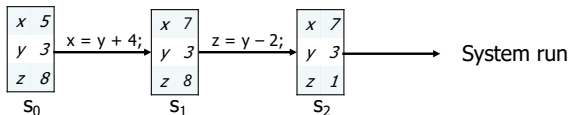
- Do traffic lights switch concurrently or interleaved?
- Each traffic light switches $r \rightarrow ry \rightarrow g \rightarrow y \rightarrow r$
- But not all states should be reachable
- Some states are “bad” (e.g. $\langle g, g \rangle$)

Semantics at Different Levels of Abstraction

- ▶ On an abstract level, the semantics of a **system** (programs running on computers) can be modelled as a FSM.
- ▶ On the **hardware level**, a single computer can be modelled as a FSM:
 - ▶ **State**: Registers, Memory
 - ▶ **Transitions**: read instruction from current PC, execute instruction.
- ▶ On the **software level**, the operational semantics of a program can be modelled as FSM:
 - ▶ **State**: Memory (Variables)
 - ▶ **Transitions**: Effects of each program statement
 - ▶ Different levels of abstraction, depending on programming language

Operational Semantics of Programs

- **States** and transitions between them:



- **Operational semantics** describes relation between states and transitions:

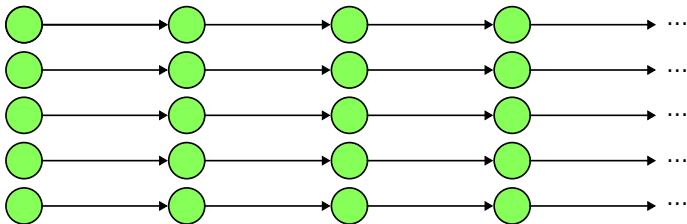
$$\frac{\langle s, e \rangle \rightarrow n}{\langle s, x = e \rangle \rightarrow s[x]^n} \quad \text{hence:} \quad \frac{\langle s_0, y + 4 \rangle \rightarrow 7}{\langle s_0, x = y + 4 \rangle \rightarrow s_1}$$

- **Formal proofs**; e.g. proving

$$\begin{array}{l} x = y + 4; \\ z = y - 2; \end{array} \text{ yields the same final state as } \begin{array}{l} z = y - 2; \\ x = y + 4; \end{array}$$

Semantics of Programs and Requirements

- ▶ Operational semantics gives us the set of all possible system runs:

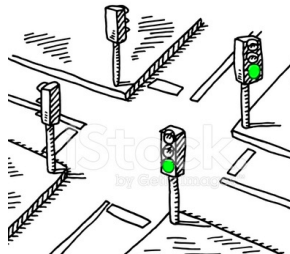


- ▶ We can now consider safety/security-related **requirements**:
 - ▶ Requirements on **single states**,
 - ▶ Requirements on **system runs**,
 - ▶ Requirements on **sets of system runs**.
- ▶ Each gives rise to different **proof methods**.

Requirements on States: Safety Properties

- ▶ Safety property S : *Nothing bad happens.*
 - ▶ i.e. system will never enter a **bad** state.
 - ▶ e.g. lights are never switched to green at the same time.
- ▶ A **bad state**
 - ▶ can be **immediately** recognized;
 - ▶ can **not** be sanitized (by following states).
- ▶ $S \in \mathcal{P}(\Sigma^\omega)$ is a **safety property** iff

$$\forall t. t \notin S \longrightarrow (\exists t_t. t_1 \in \Sigma^* \wedge t_1 \leq t \longrightarrow \forall t_2. t_1 \leq t_2 \longrightarrow t_2 \notin S)$$



Proving Safety Properties

- ▶ In the previous specification, t_1 is **finite**, Hence:
 - ▶ a property is a safety property iff its violation can be detected on a finite trace.
 - ▶ Thus, the **violation** of safety properties can be detected by **testing** (and model-checking).
- ▶ Safety properties are typically proven by **induction**:
 - ▶ Base case: initial states are good.
 - ▶ Step case: each possible transition from a good state leads to a good state.
- ▶ Safety properties can be enforced by **run-time monitors**:
 - ▶ Monitor checks following state in advance, and allows execution only if it is a good state.

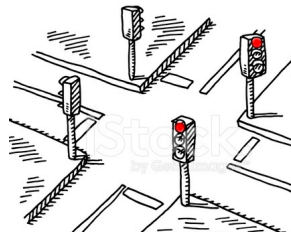
Requirements on Runs: Liveness Properties

- ▶ Liveness property S: *Good things will happen eventually**.
 - ▶ I.e. System will at some point enter a **good** state.
 - ▶ E.g. Traffic lights will eventually go green.
- ▶ A **good state**
 - ▶ is always possible, but
 - ▶ potentially infinite (i.e. no upper bound on when it will occur).
- ▶ $L \in \mathcal{P}(\Sigma^\omega)$ is a **liveness property** iff

$$\forall t. t \in \Sigma^* \implies \exists t_1. t \cdot t_1 \in L$$

- ▶ i.e. all finite traces can be extended to a trace in L.

* NB: *eventually* bedeutet *irgendwann* oder *schlussendlich* aber **nicht** *eventuell*.

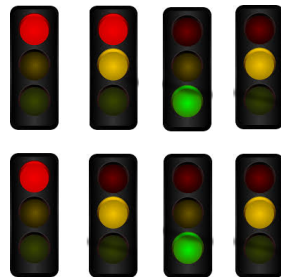


Proving Liveness Properties

- ▶ Liveness properties **cannot** be **enforced** by run-time monitors.
- ▶ Liveness properties **cannot** be checked by **testing**.
- ▶ Liveness properties are typically proven by the help of well-founded orderings:
 - ▶ Define measure function μ on states S : $\mu : S \rightarrow X$ with (X, \preceq) well founded.
 - ▶ Show each transition decreases μ : if $s_1 \rightarrow s_2$ then $\mu(s_2) \preceq \mu(s_1)$
 - ▶ If $\mu(t)$ minimal in \preceq then $t \in S$
- ▶ Example:
 - ▶ Ordering $(X, \preceq) = (\mathbb{N}, \leq)$
 - ▶ Measure denotes the number of transitions until light goes green.

Requirements on Sets of Runs: Safety Hyperproperties

- ▶ Safety hyperproperty S : **System never behaves bad.**
 - ▶ No bad thing happens in a finite set of traces;
 - ▶ (prefixes of) different system runs do not exclude each other;
 - ▶ E.g. Traffic light cycle is always the same.
- ▶ A **bad system** can be recognized by a bad observation (set of finite runs)
 - ▶ A bad observation cannot be sanitized by adding additional runs.
 - ▶ E.g. two system runs having different traffic light cycles.
- ▶ $S \in \mathcal{P}(\mathcal{P}(\Sigma^\omega))$ is a **safety hyperproperty** iff



$$\forall T. T \notin S \longrightarrow (\exists Obs. Obs \in \mathcal{P}_{fin}(\Sigma^*) \wedge Obs \leq T \longrightarrow \forall T'. Obs \leq T' \longrightarrow T' \notin S)$$

(Same as safety property but we talk about sets of traces here!)

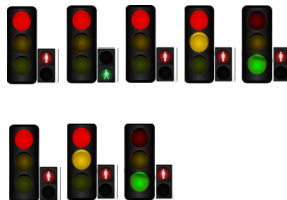
- ▶ Examples: Non-interference

Requirements on Sets of Runs: Liveness Hyperproperties

- ▶ Liveness hyperproperty S : *The system will eventually evolve to a good system.*
 - ▶ Considering any finite part of system behaviour, the system eventually develops into a good system (by extending runs, or adding new runs)
 - ▶ E.g. Green lights for pedestrians can always be omitted.
- ▶ $L \in \mathcal{P}(\mathcal{P}(\Sigma^\omega))$ is a **liveness hyperproperty** iff

$$\forall T. T \in \mathcal{P}(\Sigma^*) \implies \exists G. G \in \mathcal{P}(\Sigma^\omega) \wedge T \leq G \wedge G \in L$$

- ▶ T is a finite set of traces
- ▶ Each observation can be completed to a system G satisfying L
- ▶ Examples: average response time, SLAs, fair scheduling



Facts about (Hyper)Properties

- ▶ Every property is an **intersection** of a **safety** and a **liveness** property.
- ▶ Every hyperproperty is an **intersection** of a **safety** and a **liveness** hyperproperty.

Conclusion & Summary

- ▶ Software development models: structure vs. flexibility
- ▶ Safety standards such as IEC 61508, DO-178C suggest V-model.
 - ▶ Specification and implementation linked by verification and validation.
 - ▶ Variety of artefacts produced at each stage, which have to be subject to external review and audits.
- ▶ Finite state machines are the most basic semantic notion.
- ▶ Requirements are formulated on basis of traces
- ▶ Safety and Security Requirements
 - ▶ Properties: sets of traces, requirements on single states or runs
 - ▶ Safety and Liveness properties
 - ▶ Hyperproperties: sets of properties, requirements on many runs
 - ▶ Safety and Liveness hyperproperties