

Korrekte Software: Grundlagen und Methoden
Vorlesung 15 vom 30.06.16: Separation Logic
Slides courtesy of Rajeev Goré, ANU, Australia

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Axiom Schemas

$$p_1 * p_2 \Leftrightarrow p_2 * p_1$$

$$(p_1 * p_2) * p_3 \Leftrightarrow p_1 * (p_2 * p_3)$$

$$p * \mathbf{emp} \Leftrightarrow p$$

$$(p_1 \vee p_2) * q \Leftrightarrow (p_1 * q) \vee (p_2 * q)$$

$$(p_1 \wedge p_2) * q \Leftrightarrow (p_1 * q) \wedge (p_2 * q)$$

$$(\exists x.p) * q \Leftrightarrow \exists x.(p * q)$$

when x not free in q

$$(\forall x.p) * q \Leftrightarrow \forall x.(p * q)$$

when x not free in q

Unsound axiom schemas

$$p \Rightarrow p * p$$

(Contraction)

$$p * p \Rightarrow p$$

(Weakening)

More valid axiom schemas

$$p_1 \wedge p_2 \Rightarrow p_1 * p_2$$

when p_1 or p_2 pure

$$p_1 * p_2 \Rightarrow p_1 \wedge p_2$$

when p_1 and p_2 pure

$$(p \wedge q) * r \Rightarrow p \wedge (q * r)$$

when p pure

Pure Expressions

An expression e is *pure*, if it does neither contain \mapsto , \rightsquigarrow nor **emp**.

Showing $x = y$

$$(6) \{x = x_1 \wedge x \mapsto v * y = y_1 \wedge y \mapsto v\} x := [x]; y = y \\ \{x = v \wedge x_1 \mapsto v * y = v \wedge y_1 \mapsto v\}$$

$$x = v \wedge x_1 \mapsto v * y = v \wedge y_1 \mapsto v$$

$$\Rightarrow x = v * x_1 \mapsto v * y = v \wedge y_1 \mapsto v \quad x = v \text{ pure}$$

$$\Rightarrow x = v * x_1 \mapsto v * y = v * y_1 \mapsto v \quad y = v \text{ pure}$$

$$\Rightarrow (x = v * y = v) * x_1 \mapsto v * y_1 \mapsto v$$

$$\Rightarrow (x = v \wedge y = v) * x_1 \mapsto v * y_1 \mapsto v \quad x = v \text{ and } y = v \text{ pure}$$

$$\Rightarrow x = y * x_1 \mapsto v * y_1 \mapsto v$$

Mutation

$$\{e \mapsto -\}[e] := e' \{e \mapsto e'\}$$

Example $[x] := \text{cpns}(3, 4)$

$$\begin{array}{ccccc} St & Hp & & x := \text{cpns}(3, 4) & St \quad Hp \\ x = 20 & 20 & 21 & & x = 20 & 20 & 21 \\ *1 & 2 & & & 3 & 4 \end{array}$$

Axiom Instance

$$\{x \mapsto 20, 21\}[x] := \text{cons}(3, 4)\{x \mapsto 3, 4\}$$

Mutation (backwards)

$$\{e \mapsto - * (e \mapsto e' -* p)\}[e] := e'\{p\}$$

Example $[x] := \text{cpns}(3, 4)$

$$\begin{array}{lll} St & Hp \\ x = 20 & 20 & 21 \\ *1 & 2 & \\ \end{array} \qquad x := \text{cpns}(3, 4) \qquad \begin{array}{lll} St & Hp \\ x = 20 & 20 & 21 \\ 3 & 4 & \end{array}$$

Axiom Instance

$$\{x \mapsto 20, 21 * (x \mapsto 3, 4 -* x \mapsto 3 \wedge x + 1 \mapsto 4)\}[x] := \text{cons}(3, 4)\{x \mapsto 3 \wedge x + 1 \mapsto 4\}$$

Summary

- ▶ Separation logic is the method to really handle point structures
- ▶ Can also handle function and procedure calls.
- ▶ Needs to be adapted for C